You know, this place makes me wonder. Which would be worse—to live as a monster, or to die as a good man?

—Teddy Daniels in Shutter Island

# THE TRIVIAL NOTIONS SEMINAR

# An "easy" case of the Zariski dense orbit conjecture

### a talk by Sina Saleh

#### ABSTRACT

The Zariski dense orbit conjecture, originally formulated by Zhang, and later refined independently by Amerik-Campana and Medvedev-Scanlon, states that given a rational self-map  $\Phi$  of a quasi-projective variety *X* defined over an algebraically closed field *K*, the following dichotomy holds: either there exists a point in *X*(*K*) with a Zariski dense orbit under  $\Phi$ , or  $\Phi$  preserves a non-constant fibration. Amerik and Campana proved the conjecture in the case where *K* is an uncountable field. However, the case of a countable algebraically closed field is still open. In this talk, I will discuss the easier case of the conjecture where *X* is assumed to be an algebraic torus (or more generally any split semiabelian variety) and  $\Phi$  is a group endomorphism composed with a translation. We will see some very interesting facts about split semiabelian varieties that help us prove the conjecture quite easily in this case.

## Friday, November 18, 2022 at 11.50am Science Center, Room 507