

“God does arithmetic.” — Gauss

The Trivial Notions Seminar  
Proudly Announces

There are no abelian varieties over  $\mathbb{Z}$

A talk by  
Lin Han

**Abstract**

In 1985, Fontaine presented a beautiful argument that there are no abelian varieties over  $\mathbb{Q}$  having good reduction at all primes. The basic idea is that if there exists such an abelian variety then investigating a related filtration of  $p^n$  torsion group schemes, we will get too many rational points on the variety, contradicting the Riemann hypothesis for finite fields. We'll start with a review of some facts about group schemes and algebraic number theory.

Thursday, February 15<sup>th</sup>, 2007  
Science Center 507 at 4:15-5:15 pm